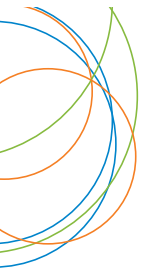




## Funding ratio attribution

Bradley Vincent-Barnes  
2023-05-11



# Funding ratio attribution

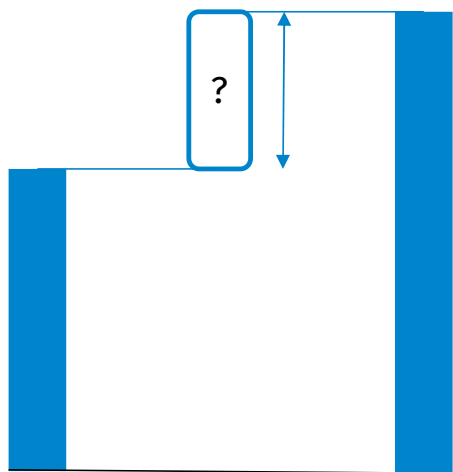
## Overview

Introduction to Funding ratio

Decomposition of ratio changes

Details

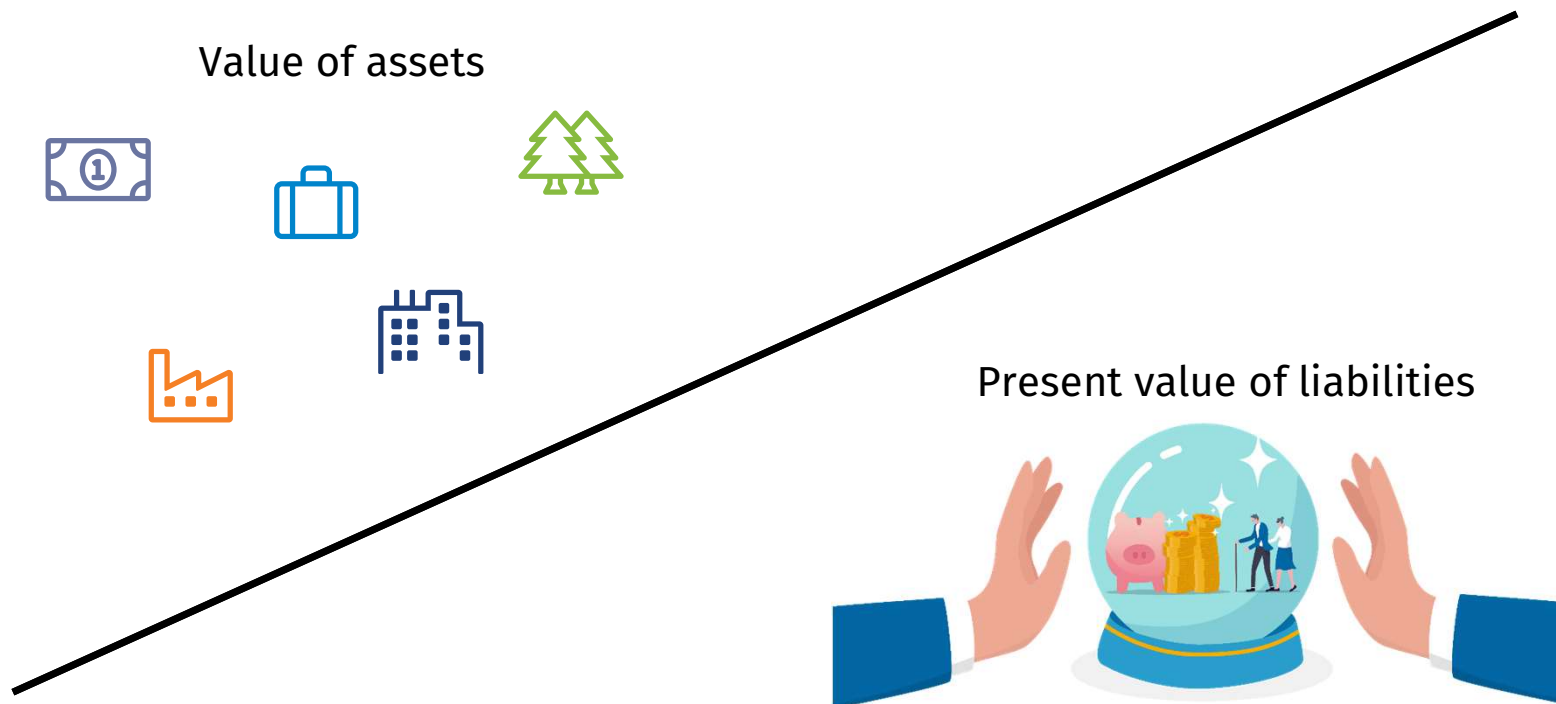
Summary





# Introduction to funding ratio

Assets and Liabilities





# Introduction to funding ratio

Why now?

- Pace of yield changes
  - 12 years down vs 2 years up
  - Faster than actuarial time frames
- Pension reform
- Negative return on assets
  - Need for greater context
- Changes in life expectancy
  - Covid
  - Cost of living
- Road to buyout

German 10 year bond yield:



United States 10 year bond yield:



Source: <http://www.worldgovernmentbonds.com>



# Introduction to funding ratio – Changes

Relation to growth of assets and liabilities

Arithmetic relation

$$\begin{aligned}\Delta \text{FundingRatio}(t, t - 1) &= \frac{\text{Assets}(t)}{\text{Liabilities}(t)} - \frac{\text{Assets}(t - 1)}{\text{Liabilities}(t - 1)} \\ &= \frac{\text{Assets}(t-1)}{\text{Liabilities}(t)} \cdot \left( \frac{\text{Assets}(t)}{\text{Assets}(t-1)} - \frac{\text{Liabilities}(t)}{\text{Liabilities}(t-1)} \right) = \text{Scaling factor} \cdot \text{XS Growth}\end{aligned}$$

Allows for use of existing investment performance frameworks

The scaling factor is a linear function, and therefore will not distort the analysis of excess growth



# Introduction to funding ratio – Changes

Relation to growth of assets and liabilities

Geometric relation

$$\Delta \text{FundingRatio}(t, t - 1) = \frac{\text{Assets}(t)}{\text{Liabilities}(t)} \bigg/ \frac{\text{Assets}(t - 1)}{\text{Liabilities}(t - 1)}$$
$$= \frac{\text{Assets}(t)}{\text{Assets}(t - 1)} \bigg/ \frac{\text{Liabilities}(t)}{\text{Liabilities}(t - 1)} = \text{Geometric XS growth}$$



# Introduction to funding ratio

Solvency ratio and defined contribution schemes

- Main line of presentation is about pension funds
  - Both open and closed schemes
- Solvency ratio from Insurance world is similar
  - Regulatory framework is more proscriptive
  - Regime specific (Fixed vs Variable for Pension funds)
- Defined contribution (DC) schemes
  - Framework not suitable when DC is additive to Defined Benefit (DB)
  - Can be used to compare when DC is substitutive (instead of DB)
    - Assets vs Annuity rates for example

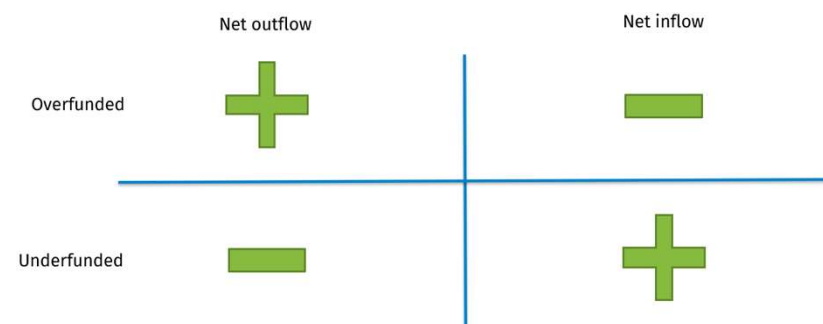


# Introduction to funding ratio - Assets

## Asset value

Asset value may change with:

- Cash flows
  - Benefit payments out (Pensions for active members)
  - Transfers (Individual)
  - Mergers and Acquisitions (Group)
  - Transfers are not neutral due to a pull towards par value
  - Somewhat discretionary within insurance
- Investment returns
  - Neutral position (Strategic Asset Allocation, SAA)
  - Investment decisions
    - Tactical Asset Allocation, TAA
    - Overlays
    - Manager Outperformance







# Introduction to funding ratio - Liabilities

Present value of liabilities

- Present value of liabilities is a function of:



Actuarial life expectancy

x



Promised retirement benefits

x



Discount rate



# Introduction to funding ratio - Liabilities

Present value of liabilities – Promised pension benefits

Promised pension benefits may change with:

- Benefit payments and new capital inflows
- Contractual adjustments (e.g. change in retirement age)
- Realized survival rate
- Realized inflation (if promise/aspiration to compensate)
- ...



# Introduction to funding ratio - Liabilities

Present value of liabilities – Discount rate

Discount rate may change with:

- Changes in expected future returns on assets
  - Regulatory framework often sets hard/soft limits
  - Expected returns for asset classes
    - Yield curve can be used for Fixed income
    - Equities and other classes are more subjective (mean regression etc.)
  
- Expected inflation (if promise/aspiration to compensate)

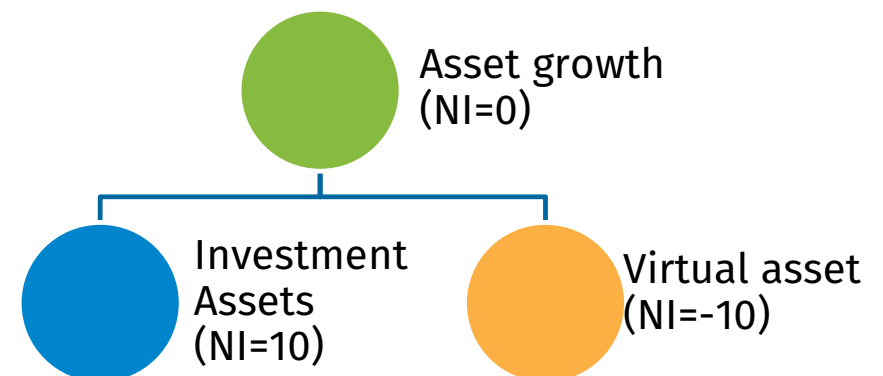


# Introduction to funding ratio – Attribution

Growth is technically the same as an investment return

- Top-down perspective:
  - Treat cash flows as autonomous components of growth/return
- Bottom-up perspective:
  - Correct for the cashflows to have actual investment returns and an investible benchmark
- Leverage existing performance attribution software

Asset value (t-1)	110
Asset value (t)	130
Growth	18.2%
Net cash flow	10
Return	9.1%





# Funding ratio attribution

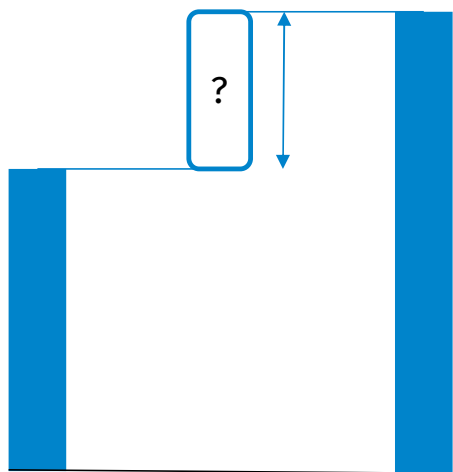
## Overview

Introduction to Funding ratio

Decomposition of ratio changes

Details

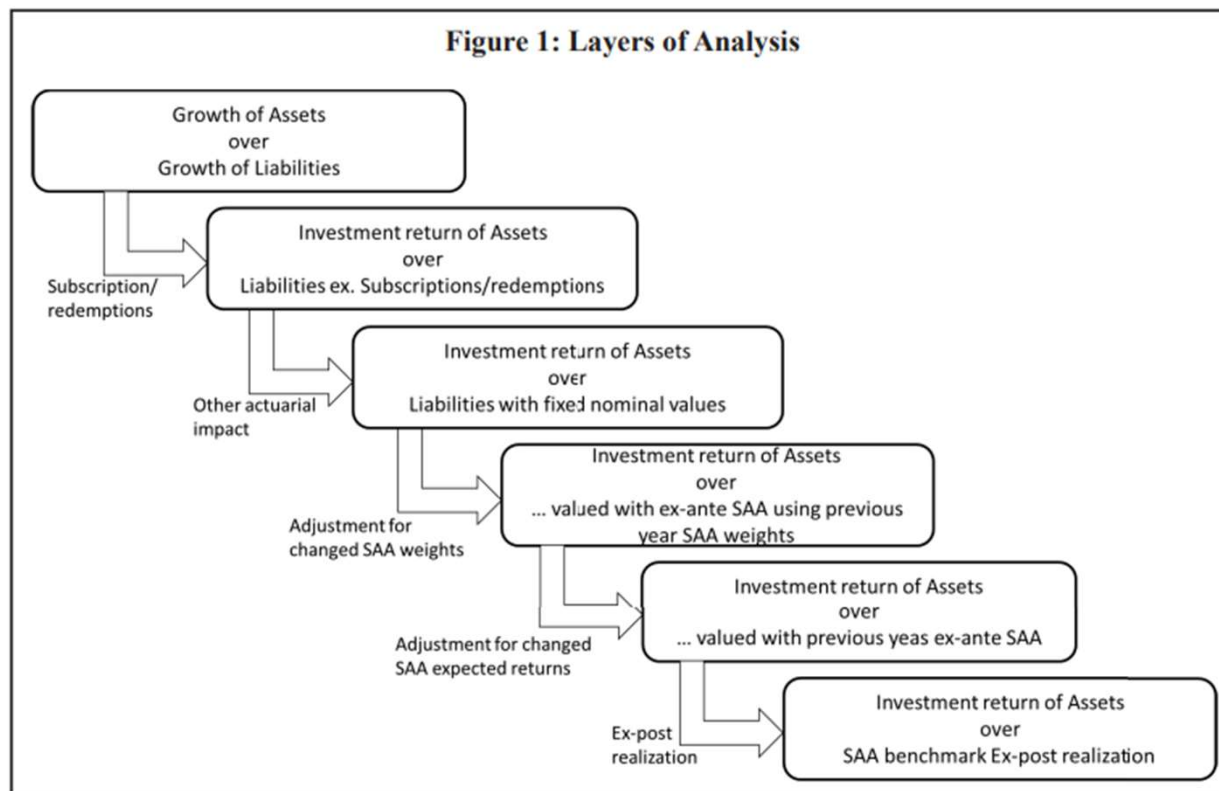
Summary





# Decomposition – Example case

Liabilities repricing

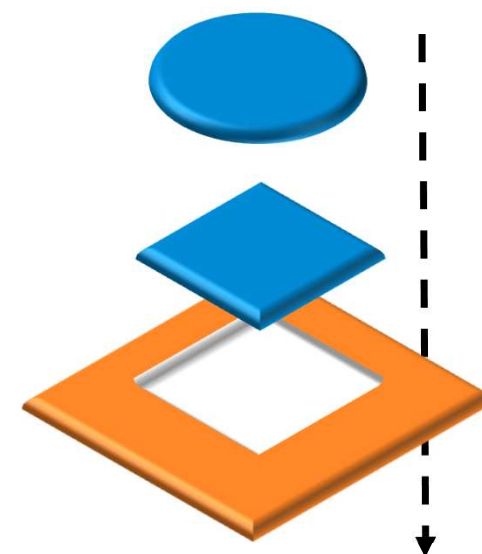


# Decomposition

Main decomposition components – and related questions

Funding ratio change can be explained by 3 categories of risk driver:

1. Explicitly not hedged
  - Actuarial factors (typically “unhedgeable”)
  - Prohibitive costs
  - Modelling risk when converting  $CPI + x \rightarrow SAA$
2. Desired exposures
  - Adherence to policy decisions (SAA)
3. Investment manager discretionary
  - Manager excess returns
  - Tactical deviations from SAA





# Decomposition – Example case

Example case introduction

	Start value	Subscriptions & Redemptions	End value
Assets	110	10	130
Liabilities	80	9	100
Funding ratio	1.375		1.30

- Nominal benefits (no inflation compensation)
- Discount rate is the SAA ex-ante expected return
  - Some fixed income exposure → Some interest rate sensitivity
- Investible benchmark is the SAA ex-post realized return





# Decomposition – Example case

## Liabilities repricing

- Transform growth in liabilities to an investible benchmark
- Liabilities are repriced for several steps of immunized risk drivers, as per decision attribution

- Evaluate liabilities under several conditions

- Normal
- Corrected for net cash flows (similar to the asset side correction)



Promised retirement benefits

Δ Cash flows

# Decomposition – Example case

Returns/growth rates to decomposition

	Start	NI	End
Assets	110	10	130
Liabilities	80	9	100
Funding ratio	1.375		1.30

Arithmetic:  
 $(9.1\% - 13.8\%) - (18.2\% - 25.0\%)$   
 $= -2.2\%$

Valuation	Assets	Liabilities	$\Delta$ Arithmetic	$\Delta$ Geometric
Top for Funding ratio	18.2% = 20/110	25.0% = 20/80		
Corrected for cash flows	9.1% = 10/110	13.8% = 11/80		

Geometric:  
 $(1.091/1.138) / (1.182/1.250) - 1$   
 $= -1.4\%$



# Decomposition – Example case

Liabilities repricing

- Evaluate liabilities under several conditions

- Normal
- Corrected for net cash flows
- Constant nominal benefits
  - In this case excluding Inflation



Promised retirement benefits

Δ Cash flows



Survival rate

Δ Other actuarial

# Decomposition – Example case

Returns/growth rates to decomposition

	Start	NI	End
Assets	110	10	130
Liabilities	80	9	100
Funding ratio	1.375		1.30

Valuation	Value
Liabilities at start	80
With cash flows	89
Actuarial impact	94

Valuation	Assets	Arithmetic	Δ Geometric
Top for Funding ratio	18.2% = 20/110	25.0% = 20/80	
Corrected for cash flows	9.1% = 10/110	13.8% = 11/80	-2.2%
Corrected for Actuarial impact	9.1%	7.5% = 6/80	

Arithmetic:  
 $(9.1\% - 7.5\%) - (9.1\% - 13.8\%)$   
 $= -6.3\%$

Geometric:  
 $(1.091/1.075) / (1.091/1.138) - 1$   
 $= -5.5\%$



# Decomposition – Example case

Liabilities repricing

- Evaluate liabilities under several conditions
  - Normal
  - Corrected for net cash flows
  - Constant nominal benefits
    - Discounted with start of period SAA asset mix
      - Accounts for intra period SAA changes
    - Discounted with start of period ex-ante SAA return
      - Forecasts are now 1 year “in the future”



Promised retirement benefits

Δ Cash flows



Survival rate

Δ Other actuarial



Discount rate

Δ SAA policy change

Δ Future expectations

# Decomposition – Example case

Returns/growth rates to decomposition

	Start	NI	End
Assets	110	10	130
Liabilities	80	9	100
Funding ratio	1.375		1.30

Valuation	Value
Liabilities at start	80
With cash flows	89
Actuarial impact	94
& SAA weights	92
& SAA returns	95

Valuation	Assets	Liabilities	Δ Arithmetic	Δ Geometric
Top for Funding ratio	18.2% = 20/110	25.0% = 20/80		
Corrected for cash flows	9.1% = 10/110	13.8% = 11/80	-2.2%	-1.4%
Corrected for Actuarial impact	9.1%	7.5% = 6/80	-6.3%	-5.5%
& SAA weights	9.1%	10.0% = (8/80)	2.5%	2.3%
& SAA returns	9.1%	6.3% = (5/80)	-3.8%	-3.4%

# Decomposition – Example case

Returns/growth rates to decomposition

	Start	NI	End
Assets	110	10	130
Liabilities	80	9	100
Funding ratio	1.375		1.30

Valuation	Value
Liabilities at start	80
With cash flows	89
Actuarial impact	94
& SAA weights	92
& SAA returns	95

Valuation	Assets	Liabilities	$\Delta$ Arithmetic	$\Delta$ Geometric
Remaining XS: The impact of actual investment decisions	18.2% = 20/110	25.0% = 20/80		
Corrected for actuarial impact	9.1% = 10/110	13.8% = 11/80	-2.2%	-1.4%
& SAA weights	9.1%	7.5% = 6/80	-6.3%	-5.5%
& SAA returns	9.1%	10.0% = (8/80)	2.5%	2.3%
Top for investments	9.1%	6.3% = (5/80)	-3.8%	-3.4%

Impact of SAA ex-ante vs ex-post:  
The realized investment climate

Remaining XS:  
The impact of actual investment decisions

9.1%      12.5%



# Decomposition – Example case

Final decomposition results

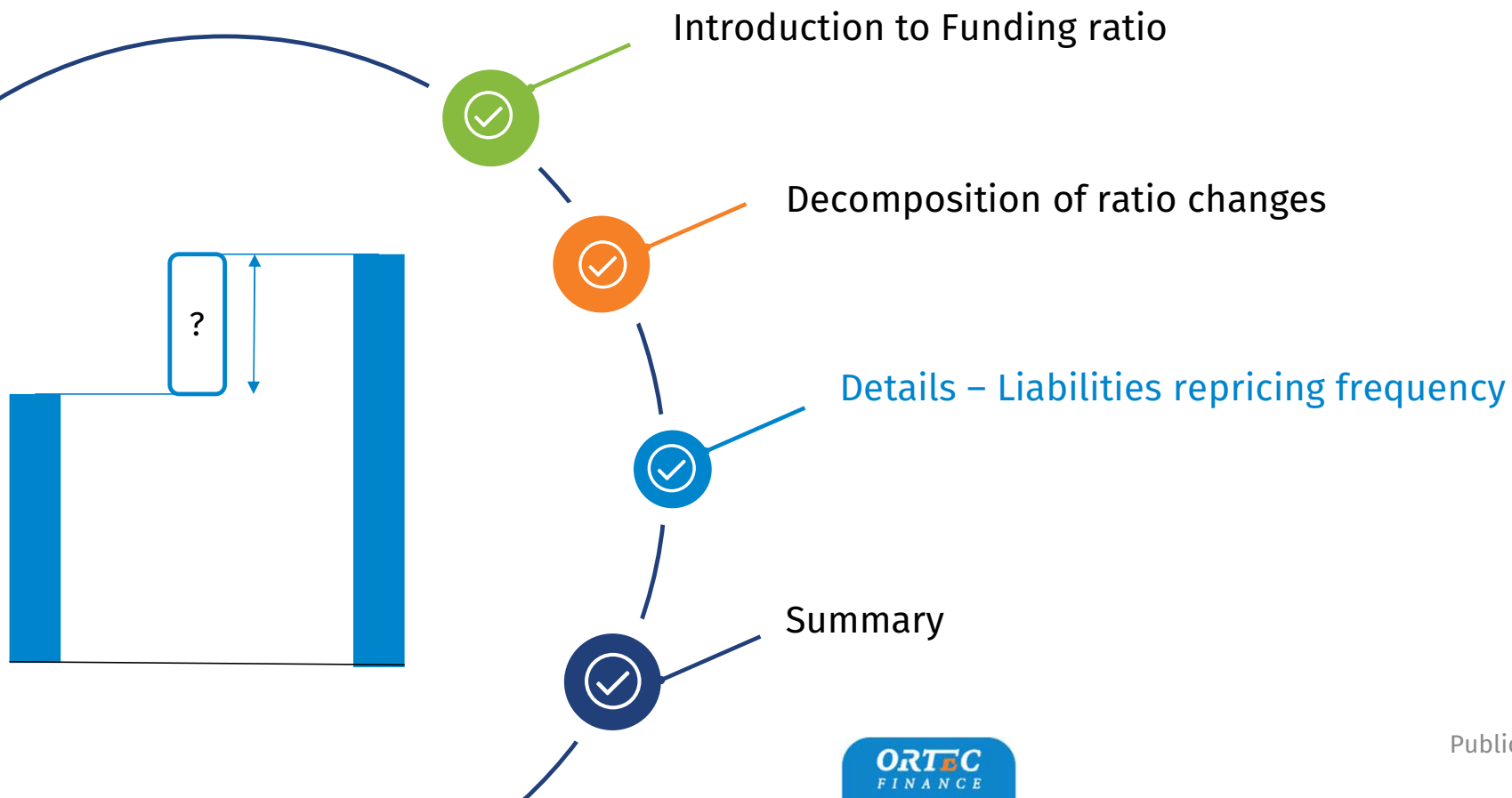
	Arithmetic	Geometric
Total funding ratio change	-7.5	-5.5
Subscriptions redemptions	-2.4	-1.4
Actuarial impact	-6.9	-5.5
Discount rate impact	-1.4	-1.2
Change in SAA policy weights	2.8	2.3
Change in expected returns	-4.1	-3.4
Investment year realization	6.9	5.9
Investment decisions	-3.8	-3.0





# Funding ratio attribution

## Overview

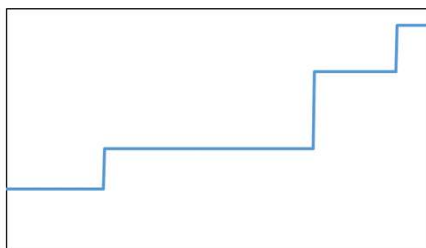


# Details – Liability repricing frequency

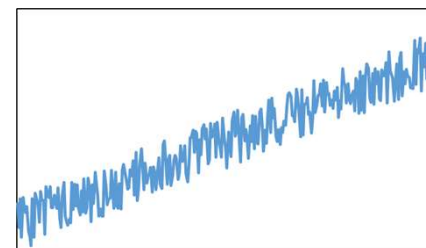
Step change vs continuous change

Growth of liabilities, may come ...

Infrequently

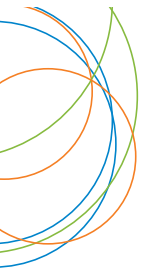


Continuously



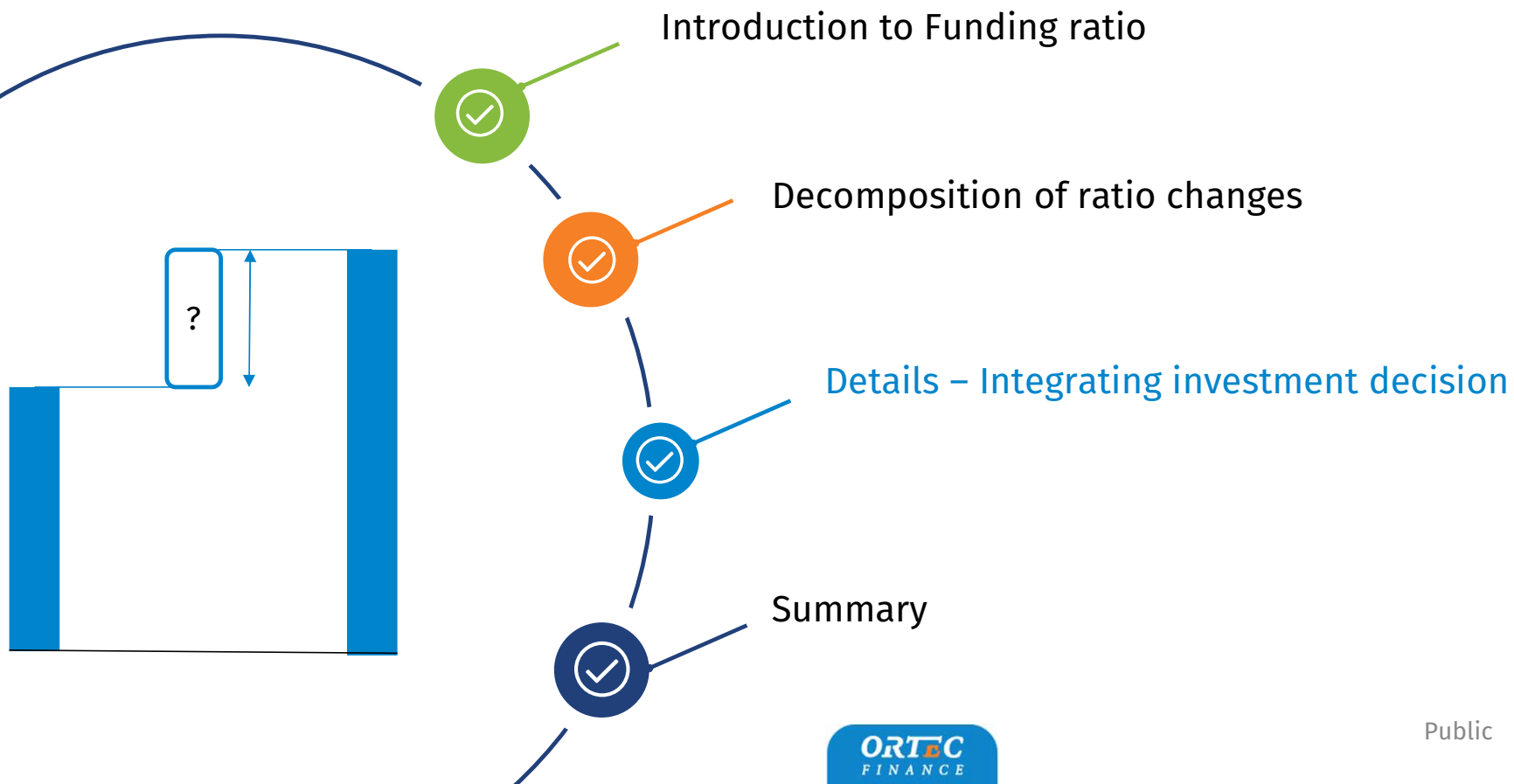
- Change in expected equity returns (> 1Y)
- Change in SAA asset-mix (> 1Y)
- Realized inflation (1Q-1Y)
- Update in life expectancy (> 1Y)
- Subscription/Redemptions (1M-1Y)
- New/Terminated business (1M-1Y)

- Asset growth is a continuous function
- Change in expected bond returns
- Change in expected inflation



# Funding ratio attribution

## Overview





# Details – Integrating investment decisions

## Investment decisions

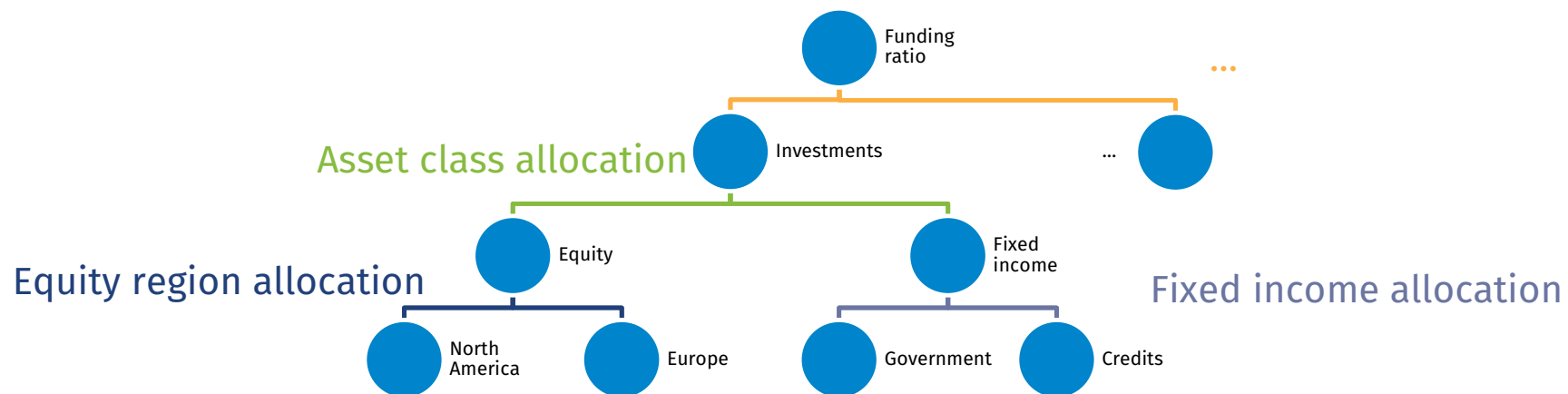
### Typical investment decisions

- Currency management
  - Strategic
  - Tactical
  
- Interest rate management
  - Strategic
  - Tactical
  
- Tactical asset mix
  
- Implementation decisions



# Details – Integrating investment decisions

Model structure





# Details – Integrating investment decisions

Micro attribution framework

	Actuarial	Asset class	EQ Region	FI Alloc
Top	-3.7	-3.4	0.7	-1.1
...	-3.7			
Investments		-3.4	0.7	-1.1
Equity		-1.9	0.7	
North America			0.5	
Europe			0.2	
Fixed income		-1.5		-1.1
Government				-0.3
Credits				-0.8



# Details – Integrating investment decisions

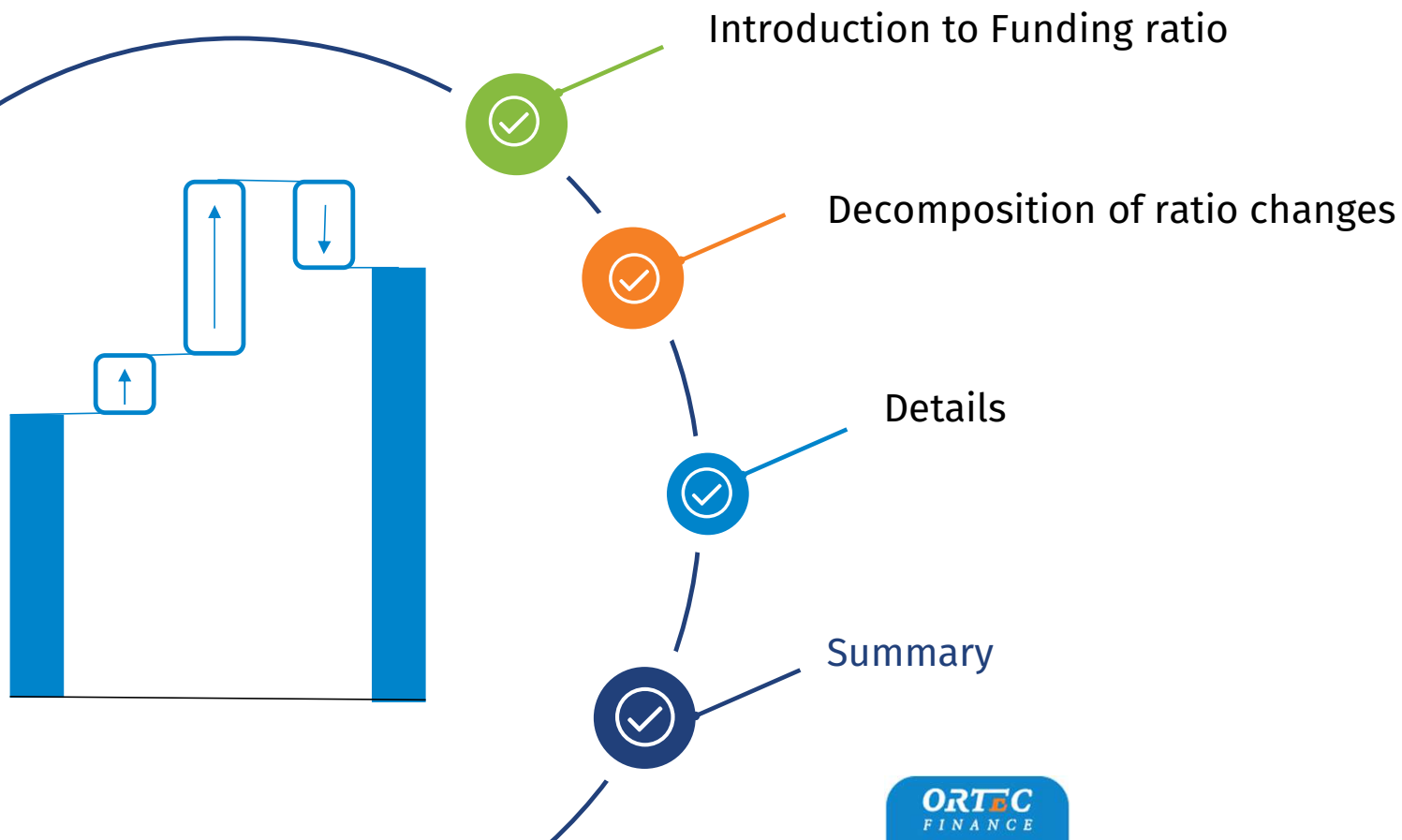
Transposed

Total funding ratio change	-7.5
Actuarial Impact	-3.7
Investment decisions	-3.8
Asset class	-3.4
EQ Region	0.7
FI Allocation	-1.1



# Funding ratio attribution

## Overview



Public





# Summary

Summary and time for questions

- Funding ratio attribution by molding data into existing formula sets
  - Treat growth as investment returns
  - Treat risk factors as investment decisions
  
- Specific circumstances require proper modelling choices
  - Solvency ratio and DC scheme differences
  - Regulatory framework
  - Model to transform discount rate into investible benchmark
  - Liability valuation frequency
  
- Questions?

# Special thanks



## Maarten Niederer

Chapter Lead

 [Maarten.Niederer@ortec-finance.com](mailto:Maarten.Niederer@ortec-finance.com)

### Background

Maarten Niederer, CFA, CIPM holds a Master degree in Computer Science from Utrecht University. Since joining Ortec Finance in 2008, Maarten has held several roles within the Investment Performance department. These roles ranged from business consultant, subject matter expert, to software developer. He is now one of the Chapter Leads for the broader organization.



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